Quantum Computation and Quantum Information (QCQI)

Programme: M.Sc./B.Tech*. Year: 2nd year/4th year Semester: 3rd/7th

Course type : Elective * Credits : 4/3 Contact Hours : 40 (+ tutorials*)

Course Context and Overview:

The world of science and technology has become highly inter-disciplinary and the field of Quantum computation and quantum information is a prime example of this. The subject combines three major revolutions of last century - the physics of quantum mechanics, the theory of computation and information theory which leads to a new paradigm of computation and information processing. A lot of theoretical and experimental effort is being made by a lot of Universities/institutions around the world as well as by companies like Google, Microsoft, IBM etc. to develop large enough quantum computers to explore the possibilities that this new paradigm of computation and information processing offers.

The course is intended to be a first course in Quantum Computation and Quantum Information (that is, no familiarity with the subject assumed). Keeping in mind the interdisciplinary nature of the subject, the students will be introduced to the basic concepts from the theory of computation which will be followed by an elementary introduction to quantum mechanics before plunging into quantum computation. After introducing the basic notions of qubits, quantum gates, entanglement etc. the students will be exposed to certain well known quantum algorithms like Shor's algorithm and Grover's algorithm which highlight the power of quantum computation in comparison to the standard computation. Finally, we look at the use of quantum concepts in information processing tasks including quantum cryptography. The various concepts will be discussed with examples.

It might not be altogether preposterous to suggest that once reasonably large quantum computers (in terms of their computational power) of manageable size are developed (which might not be too many years in the future given the amount of effort being made), the present day computers would become a thing of past. A first exposure to the subject is therefore desirable of students at master's level or final year undergraduate level as this might motivate them to explore the field further and even otherwise, once quantum computers become a commercial possibility, the initial exposure would mean that the subject would not be completely alien to them.

Prerequisites:

Linear algebra is the only real prerequisite for the course (we will nevertheless discuss linear algebra in brief). Exposure to any or all of the following subjects - quantum mechanics, theory of computation and information theory - though not necessary will be helpful.

On completion of this course

CO1: Students would have a broad overview of the theory of computation and information theory and an appreciation of how the relevant notions might depend on the underlying physics.

CO2: Students should have a working knowledge/understanding of simple finite dimensional quantum systems.

CO3: Students should be able to analyze simple quantum circuits.

CO4: With some effort students should be able to translate between quantum circuits and quantum algorithms.

CO5: Students should develop an understanding/appreciation for how quantum physics (and quantum entanglement) might give an edge over classical information theory and classical cryptography.

Course Topics:

Topics	No. of lectures (approximate**)
Introduction	1
Introduction to some basic concepts in the theory of computation (including Turing machines and the circuit model of computation, reversible computers)	6-7
Introduction to basics of quantum mechanics (including linear algebra)	6-7
Preliminary notions in quantum computation – qubits and quantum gates, single qubit quantum systems (including measurement) and application to quantum key distribution, no cloning theorem	4-5
Multiple-qubit systems – tensor product space, quantum entanglement, multi-qubit quantum gates and quantum circuits – reversible and quantum versions of simple gates, controlled gates and universal gates, quantum versions of classical computations, EPR paradox and Bell states, applications to quantum dense coding and quantum teleportation,	5-6
Simple quantum algorithms – Deutsch algorithm, Deutsch-Jozsa problem, Bernstein-Vazirani problem, Simon's problem	2-3
Quantum Fourier transform and Shor's factoring algorithm	3-4
Grover's algorithm	2
Physical realization of quantum computers	3-4
Quantum error correction, quantum information and quantum cryptography***	10
Total***	42-49

^{*} Considering the nature of the course, it is open for master's students in Physics and maths and for M.Tech. and B.Tech. final year students from CSE, CCE and ECE. However, motivated students from MME can also take this course if they wish. Note that the tutorials are compulsory for master's students and optional for B.Tech. Students.

Text Books:

- 1. Quantum Computing: A Gentle Introduction E. Rieffel and W. Polak (The MIT Press).
- 2. Quantum Computer Science: *An Introduction* N. David Mermin (Cambridge University Press).
- 3. An Introduction to Quantum Computing P. Kaye, R. Laflamme and M. Mosca (Oxford Univ. Press).
- 4. Quantum Computing Explained D. Mcmahon (Wiley India Pvt. Ltd.).

^{**} I find it difficult to make a precise statement regarding the number of lectures required for a particular topic. It depends on my delivery and students' grasping.

^{***} At present I am not sure as to exactly what topics to cover in this part and in how much detail. As per the present estimate, the total number of lectures is also more than forty. The picture will become clear once the course is underway and we know how well we are progressing. At that later stage more details regarding this part will be supplied.

Reference Books:

- 1. Quantum Computation and Quantum Information M.A. Nielsen and I.L. Chuang (Cambridge Univ. Press).
- 2. Classical and Quantum Computation A. Yu. Kitaev, A.H. Shen and M.N. Vyalyi (Graduate Studies in Mathematics, AMS) (Indian edition by Universities Press).

Additional Resources:

- 1. Online lecture notes of John Preskill's course on Quantum Computation can be found at http://www.theory.caltech.edu/people/preskill/ph229/
- 2. Online edX lectures on Quantum Information Science by Issac Chuang and Peter Shor can be found at https://www.edx.org/course/quantum-information-science-i and

https://www.edx.org/course/quantum-information-science-i-part-2-mitx-8-370-2x

Evaluation:

Item	Weightage
3-4 quizzes	25
1 midterm	25
1 endterm	50

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